Rational Equations

Procedure
1. **Find the common denominator (CD) by factoring the denominators**
2. **Multiply both sides of the equation by the CD**
3. **Solve the resulting equation**
4. **Check your solution**

Example $\dfrac{4}{x+2} - \dfrac{2}{x-2} = \dfrac{-x}{x-2}$

1. CD $= (x+2)(x-2)$
2. $(x+2)(x-2)\left[\dfrac{4}{x+2} - \dfrac{2}{x-2}\right] = (x+2)(x-2)\left[\dfrac{-x}{x-2}\right]$
3. $4(x-2) - 2(x+2) = -x(x+2)$
   $4x - 8 - 2x - 4 = -x^2 - 2x$
   $2x - 12 = -x^2 - 2$
   $x^2 + 4x - 12 = 0$
   $(x+6)(x-2) = 0$
   $x = -6$ or $x = 2$

 # x cannot be 2, makes the denominator 0, $\therefore x = -6$

1. $\dfrac{x}{x-6} = 3$

2. $\dfrac{x}{x-4} = 5$

3. $\dfrac{2x}{x-2} = \dfrac{5}{3}$

4. $\dfrac{x-3}{x+7} = 6$

5. $\dfrac{6}{x-1} + \dfrac{10}{x+1} = \dfrac{60}{x^2-1}$

6. $\dfrac{x}{x-2} + \dfrac{2}{x+2} = \dfrac{x^2+4}{x^2-4}$

7. $\dfrac{4x+3}{x^2-x-6} + \dfrac{x-4}{x=3} = \dfrac{x}{x-3}$

8. $\dfrac{2x+1}{x+1} - \dfrac{3x}{x-2} = \dfrac{5x-2}{x^2-x-2}$

9. $\dfrac{2x+1}{x-1} - \dfrac{3x}{x+2} = \dfrac{5x-2}{x^2+x-2}$

10. $\dfrac{x+6}{x-5} + \dfrac{x+2}{x-2} = \dfrac{x^2+20}{x^2-7x+10}$

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