

Transformations by Definition

Translation – a translation that maps point X into X' maps every point P into P' such that:

- If P does not lie on $\overleftrightarrow{XX'}$, then $PXX'P'$ is a parallelogram.
- If P lies on XX' , then there is a segment $\overline{YY'}$, such that both $XYY'X'$ are parallelograms.

Notation: $T_{XX'}(x, y) \rightarrow (x + a, y + b)$ (moving points on the coordinate axes)

The composition of two reflections over parallel lines has the same effect as a translation twice the distance between the parallel lines.

Reflection in a Line – a reflection in a line k maps every point P into a point P' such that:

- If P does not lie on k , the k is the perpendicular bisector of $\overline{PP'}$.
- If P lies on k , then P' is the same point as P .

Notation: $R_{x\text{-axis}}(x, y) \rightarrow (x, -y)$, some books use M (mirror) instead of R .

Composition of a reflection over intersecting lines is the same as a rotation (twice the measure of the angle formed by the intersecting lines)

Rotation about a point O – a rotation about a point O through \mathcal{B}° maps every point P into P' , such that:

- If P is different from O , the $OP' = OP$ and the $m\angle P'OP = \mathcal{B}^\circ$
- If P is the point O , then P' is the same as O .

Notation: $R_{O, 90^\circ}(x, y) \rightarrow (-y, x)$ (draw circles with center O thru pts, then use \mathcal{B}°)

Every rotation about a point O through \mathcal{B}° is equal to the composition of two reflections.