

Using the Rules of Exponents Theorem

Since $b^{y_1} = b^{y_2}$ iff $y_1 = y_2$.

That implies that $\log_b x_1 = \log_b x_2$ iff $x_1 = x_2$