Theorem When 2 secants intersect in a circle, the $\angle$ formed is $=$ to $\frac{1}{2}$ the sum of the arcs formed by the vertical $\angle$.

Given: XY \& ZW intersect
Prove: $\angle 1=\frac{1}{2}(\widehat{\mathrm{XZ}}+\widehat{\mathrm{YW}})$


| Statements | Reasons |  |
| :--- | :--- | :--- |
| 1. | Draw $\overline{X W}$ | Construction |
| 2. | $\angle 1=\angle 2+\angle 3$ | Ext $\angle$ of $\Delta=$ sum of 2 remote int $\angle$ 's |
| 3. | $\angle 2=\frac{1}{2} \overparen{\mathrm{ZX}}$ | Inscribed $\angle=\frac{1}{2}$ intercepted arc |
|  | $\angle 3=\frac{1}{2} \overparen{\mathrm{YW}}$ |  |
| 4. | $\angle 1=\frac{1}{2} \overparen{\mathrm{ZX}}+\frac{1}{2} \overparen{\mathrm{YW}}$ | Substitution in step 2 |
| 5. | $\angle 1=\frac{1}{2}(\widetilde{\mathrm{ZX}}+\overparen{\mathrm{YW}})$ | Distributive Prop |
|  |  |  |

Notice the importance of the triangle theorems in these proofs.

