When two chords intersect within a circle, the product of the lengths of the segments of one chord is equal to the product of the lengths of the other chord.


$$
\mathrm{ab}=\mathrm{cd}
$$

## Let's look at the proof

Given: Chords $\overline{X Y} \& \overline{Z W}$
Prove: $\mathrm{a} \cdot \mathrm{b}=\mathrm{c} \cdot \mathrm{d}$


Reasons

|  | Statements | Reasons |
| :---: | :---: | :---: |
| 1. | Draw $\overline{\mathrm{XZ}}$ and $\overline{\mathrm{WY}}$ | Construction |
| 2. | $\begin{aligned} & \angle \mathrm{X} \cong \angle \mathrm{~W} \\ & \angle \mathrm{Z} \cong \angle \mathrm{Y} \end{aligned}$ | Inscribed $\angle$ 's intercept same arc |
| 3. | $\angle \mathrm{XKZ}$ and $\angle \mathrm{YKW}$ are Vert $\angle$ | Def. Vertical $\angle$ |
| 4. | $\Delta \mathrm{XKZ} \sim \Delta \mathrm{WKY}$ | AA Postulate |
| 5. | $\frac{\mathrm{a}}{\mathrm{~d}}=\frac{\mathrm{c}}{\mathrm{~b}}$ | $\sim \Delta$ 's proportion |
| 6. | $\mathrm{ab}=\mathrm{cd}$ | Prop of Proportion |

