

# Circles

**General Equation**

$$x^2 + y^2 + ax + by + c = 0$$

**Center Form**

$$(x - h)^2 + (y - k)^2 = r^2$$

**Ex. Rewrite the equation in Center form**

$$x^2 + y^2 + 6x - 4y - 3 = 0$$

$$x^2 + 6x + y^2 - 4y = 3$$

$$x^2 + 6x + \underline{\quad} + y^2 - 4y + \underline{\quad} = 3$$

$$3 \qquad -2$$

$$x^2 + 6x + 9 + y^2 - 4y + 4 = 3 + 9 + 4$$

$$(x + 3)^2 + (y - 2)^2 = 16$$

Rewrite

Complete Sq notation

½ and sq, & add both sides

Factor

Center (-3, 2), radius 4

Given the center and radius, write an equation of a circle in Center-radius form

1. (2, 6) and  $r = 5$

2. (3, -2) and  $r = 3$

3. (-9, -3) and  $r = 4$

4. (-5, 0) and  $r = 2$

Rewrite the following equations in Center Radius form and graph.

5.  $x^2 + y^2 - 6x = 0$

6.  $x^2 + y^2 - 4x + 2y - 4 = 0$

7.  $x^2 + y^2 + 6x - 8y - 9 = 0$

8.  $4x^2 + 4y^2 - 4x - 12y + 9 = 0$

9. Find an equation of a circle with a diameter having endpoints (-2, 5) and (10, -1).

10. Graph  $x^2 + y^2 - 6x + 10y - 2 < 0$